

# A Delay Modeling Framework for Embedded Virtual Network Function Chains in 5G Networks

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## Abstract

With the development of software-defined networking (SDN) and network function virtualization (NFV), software-defined topology (SDT) design poses technical challenges in embedding virtual network function (VNF) chains to minimize the embedding cost under packet delay constraints. In this article, we present a novel E2E delay modeling framework for embedded VNF chains to facilitate the delay-aware SDT design. A resource allocation policy called dominant-resource generalized processor sharing (DR-GPS) is applied among multiple VNF chains embedded on a common physical network path to achieve dominant resource allocation fairness and high system performance. An approximated M/D/1 queueing network model is then developed to analyze the average E2E packet delay for each traffic flow traversing an embedded VNF chain.

## 1. Introduction

The fifth generation (5G) communication networks are evolving to interconnect a massive number of miscellaneous end devices with diversified service types for Internet-of-Things (IoT) [1]. Machine-to-machine (M2M) communication services and high data rate broadband services are two typical IoT service categories with different traffic statistics and customized end-to-end (E2E) delay requirements. To accommodate an increasing traffic volume from massive IoT devices with differentiated quality-of-service (QoS) demands, the number of network servers providing different functionalities, e.g., firewalls, domain name system (DNS), needs to be increased for boosted network capacity. However, the densified network deployment largely augments both capital and operational expenditure. Software-defined networking (SDN) [2] and network function virtualization (NFV) [3] are two complementary technologies to enhance global resource utilization and to reduce the network deployment cost for service customization, respectively. For the core network, the SDN control module determines the routing path for each service flow based on global network state information. A service (traffic) flow refers to aggregated traffic from a group of end devices belonging to the same service type and traversing the same source and destination edge switches. On the other hand, a centralized NFV control module exists to orchestrate virtual network functions (VNFs) at appropriate general purpose network servers (also named NFV nodes) to achieve flexible service customization. The SDN and NFV control

modules are combined as an SDN-NFV integrated controller for VNF orchestration and placement, and traffic routing decisions. At the service level, each service flow is required to pass through a specific sequence of VNFs to fulfill an E2E service delivery with certain functionality and customized QoS requirement. For example, a DNS service flow traverses a firewall function and a DNS function sequentially. A video traffic flow passes through a firewall function and an intrusion detection system (IDS) for a secured E2E video conferencing. We call a set of VNFs interconnected by virtual links as a VNF chain. Software-defined topology (SDT) design studies how to embed each VNF chain onto the physical substrate network to minimize the VNF deployment and operational cost [4].

## 2. Delay-Aware SDT Design

For the SDT design, a joint routing and VNF placement problem can be formulated as a mixed integer linear programming (MILP) problem, and a low complexity heuristic algorithm is proposed to solve the problem [4]. The SDT output is the optimal VNF placement on NFV nodes and the optimal traffic routing paths among embedded VNFs. There is an essential tradeoff between minimizing the embedding cost and satisfying the E2E packet delay requirements. To reduce the embedding cost and improve the resource utilization, different VNF chains are preferred to be embedded on a common physical network path with multiple VNFs operated on an NFV node, as shown in Fig. 1. However, the E2E packet delay for each embedded VNF chain can be degraded

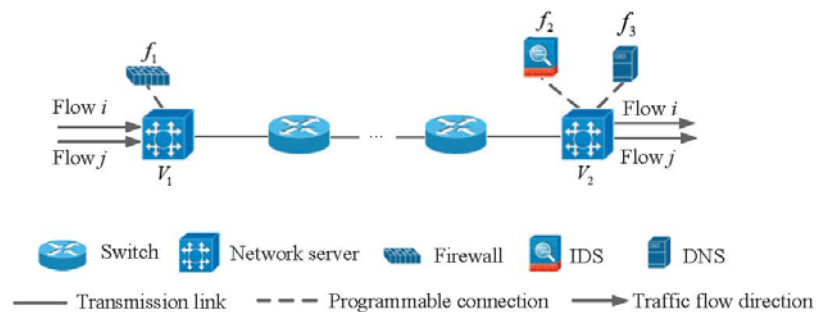


Fig. 1: Multiple VNF chains embedded on a common physical network path.

as it shares both computing and bandwidth resources with other VNF chains. Existing studies model the E2E packet delay of a traffic flow traversing an embedded VNF chain as the summation of packet transmission delays over each embedded virtual link, without considering the packet processing delay at each NFV node [3], [5]. As a matter of fact, when each packet of a traffic flow traverses an embedded VNF on an NFV node, the packet requires an amount of CPU processing time for certain functionality and an amount of packet transmission time on the outgoing link sequentially. Depending on the type of traversed VNF and the type of service that each flow belongs to, different flows have discrepant time consumption for both CPU processing and link transmission. Some small packets with large header size (e.g., DNS request packets) demand more CPU processing time, whereas other packets with large packet size (e.g., video packets) consume more link transmission time. Therefore, how to allocate both computing and bandwidth resources among the flows traversing the VNF(s) embedded on a common NFV node needs

investigation, which affects the packet delay of each flow. More importantly, a comprehensive E2E delay model for packets of a service flow passing through each embedded VNF chain should be established, with the joint consideration of packet processing delays on NFV nodes and packet transmission delays on physical links and network switches (see details in Section III), to achieve delay-aware SDT design.

### 3. E2E Packet Delay Modeling

When traversing an embedded VNF, each traffic flow, say flow  $i$ , requires different amounts of packet processing time and packet transmission time, denoted by  $[t_{i,1}, t_{i,2}]$ . We refer to this time vector as *time profile*. We define the resource type that a traffic flow consumes more in processing or transmitting one packet as *dominant resource*. Since different service flows have discrepant time profiles when passing through the VNF(s) on an NFV node, a *dominant resource generalized processor sharing (DR-GPS)* scheme [6] is employed to allocate the CPU processing resources and the transmission bandwidth resources among different flows. Compared with GPS [7], the DR-GPS is a promising strategy in the context of bi-resource allocation to balance the trade off between fair allocation and high resource utilization. If GPS is directly applied for the bi-resource allocation (i.e., bi-resource GPS), where both processing and transmission rates are equally partitioned among different service flows, the system performance can be degraded due to the discrepancy of time profiles of different flows. In DR-GPS, the fractions of dominant resources allocated to multiple backlogged flows at an NFV node are equalized to ensure the allocation fairness on the dominant resource types (i.e. dominant resource fairness). The fraction of non-dominant resources is allocated to each backlogged flow in proportional to its time profile to eliminate the packet queueing delay before link transmission. When a traffic flow at an NFV node has no packets waiting for processing and transmission, its allocated resources are redistributed among other backlogged flows according to DR-GPS, to improve resource utilization via traffic multiplexing. With the DR-GPS, the processes of packets from each flow traversing the first NFV node  $V_1$  of an embedded network path can be modeled as a tandem queueing system, as shown in Fig. 2, where a set of flows traverse  $V_1$  and the traffic arrival process for flow  $i$  is modeled as a Poisson process with the arrival rate  $\gamma_i$ . The processing and transmission rates allocated to flow  $i$  are  $r_{i,1}$  and  $r_{i,2}$ , where we have  $r_{i,1} = r_{i,2}$  according to the DR-GPS. Thus, there is no packet queueing before the link transmission, and packet queueing exists only before the CPU processing.

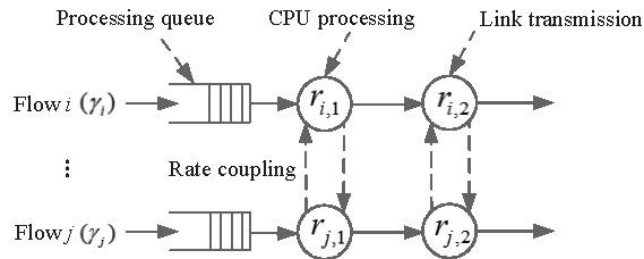


Fig. 2: A tandem queueing model for traffic flows traversing  $V_1$ .

Given the set of flows multiplexing at an NFV node, the instantaneous packet processing rate of a tagged flow varies among a set of discrete rate values, depending on the non-empty queueing states of the other flows. This rate correlation makes the queueing analysis intractable for delay calculation. For tractability, we calculate the average packet processing rate for each flow by taking into account the processing queue non-empty probabilities of all the other traffic flows (i.e., exploiting the traffic multiplexing gain), which is used as an approximation of decoupled packet processing rate for the flow [1]. Then, a decoupled queueing model for packet processing of each traffic flow at  $V_1$  is established, where the decoupled processing rate for flow  $i$  is denoted by  $d_{i,1}$ , as shown in Fig. 3. To further decouple the transmission rate correlation, we analyze the packet departure process from each decoupled processing at  $V_1$ . Let  $X_i$  be the packet inter-departure time of flow  $i$  at the decoupled processing of  $V_1$ . Due to the Poisson characteristics of the packet arrival process, a departing packet sees the same steady-state queue occupancy distribution as an arriving packet [8]. Therefore, if the  $m$  th departing packet sees a non-empty queue, we have  $X_i = T_i$ , where  $T_i = \frac{1}{d_{i,1}}$ ; if the packet sees an empty queue, we have

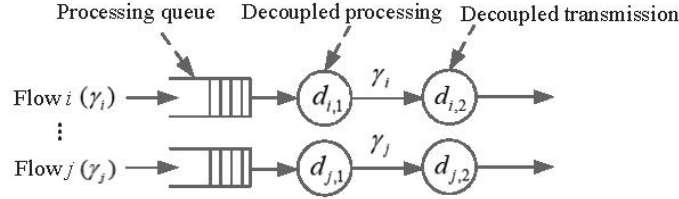


Fig. 3: A queueing model for decoupled packet processing and transmission [1].

$X_i = T_i + Y_i$ , where  $Y_i$  is the duration from the  $m$  th packet departure instant to the arrival instant of the  $(m+1)$  th packet of flow  $i$ . Due to the memoryless property,  $Y_i$  follows the same exponential distribution as the packet inter-arrival time. Therefore, the probability density function (PDF) of  $X_i$  can be calculated as

$$\phi_{X_i}(t) = (1 - \rho_{i,1})\phi_{(Y_i+T_i)}(t) + \rho_{i,1}\phi_{T_i}(t) \quad (1)$$

where  $\rho_{i,1} = \frac{\gamma_i}{d_{i,1}}$ ,  $\phi_{(Y_i+T_i)}(t)$  and  $\phi_{T_i}(t)$  are the PDFs of  $(Y_i + T_i)$  and  $T_i$ , respectively. As  $T_i$  and  $Y_i$  are independent variables,  $\phi_{(Y_i+T_i)}(t)$  can be calculated as the convolution of the PDFs of  $Y_i$  and  $T_i$  [1]. Then, the cumulative distribution function (CDF) of  $X_i$ , and its mean and variance are further expressed as [1]

$$\varphi_{X_i}(t) = \left[ 1 - \left( 1 - \frac{\gamma_i}{d_{i,1}} \right) e^{-\gamma_i(t-T_i)} \right] u(t-T_i), \quad (2)$$

$$E[X_i] = \frac{1}{\gamma_i}, \quad \text{and} \quad D[X_i] = \frac{1}{\gamma_i^2} - \frac{1}{d_{i,1}^2}. \quad (3)$$

Eq. (2) and Eq. (3) indicate that the packet inter-departure process from the decoupled processing is a general process between a Poisson process and a deterministic process, with the average departure rate  $\gamma_i$ . Therefore, by using the same method as the processing rate decoupling, we calculate the decoupled packet transmission rate for flow  $i$  as  $d_{i,2}$ , where  $d_{i,2} = d_{i,1}$ . This is because the instantaneous processing and transmission rates are equalized according to DR-GPS, i.e.,  $r_{i,1} = r_{i,2}$ , and the average departure rate from each decoupled processing is same as the arrival rate. With the completely decoupled queueing model for both packet processing and packet transmission, the average packet delay,  $D_{i,1}$ , for traffic flow  $i$  traversing the first NFV node can be determined [1], including packet queueing delay before processing, decoupled packet processing delay, and decoupled packet transmission delay, according to the M/D/1 queueing analysis.

Before modeling the delay of packets traversing the second NFV node  $V_2$ , we first analyze the packet departure process from the decoupled link transmission of flow  $i$  at  $V_1$ , which is derived as the same general process with the departure process from the decoupled processing (Analytical details are provided in [1]). The process approaches a Poisson process when  $\gamma_i$  is small and a deterministic process when  $\gamma_i$  is large. Packets from each decoupled outgoing link transmission are then forwarded through a number of network switches and physical links before arriving at the subsequent NFV node. According to Proposition 1 in [1], the packet arrival process of a traffic flow at  $V_2$  is the same as the departure process from  $V_1$ , as long as the transmission rate allocated to the flow at each traversed network switch and link is greater than or equal to the decoupled transmission rate at  $V_1$ . In this way, no queueing delays are incurred on switches and links, and the bandwidth utilization is maximized. The delay over the embedded virtual links between  $V_1$  and  $V_2$  can be calculated as the summation of packet transmission delays over network switches and physical links between  $V_1$  and  $V_2$  [1]. Since the packet arrival process of each flow at  $V_2$  is the same general process in between a Poisson process and a deterministic process with the average rate  $\gamma_i$ , we decouple the processing and transmission rates for flow  $i$  at  $V_2$ , similar to the rate decoupling at  $V_1$ . The decoupled rates are denoted by  $d'_{i,1}$  and  $d'_{i,2}$ , as shown in Fig. 4, where  $d'_{i,1} = d'_{i,2}$ .

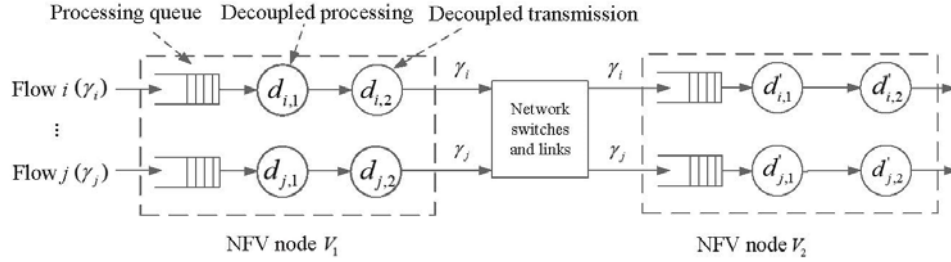


Fig. 4: A decoupled queueing model for traffic flows traversing  $V_1$  and  $V_2$  in sequence.

Since the traffic arrival process at  $V_2$  correlates with the packet processing and transmission at  $V_1$ , a G/D/1 queueing model is not accurate for calculating the delay of packets going through each decoupled processing at  $V_2$ , especially when  $\gamma_i$  is large [8]. For the case of  $d'_{i,1} < d_{i,2}$ , the traffic arrival process of each flow at  $V_2$  is more likely to approach a Poisson process with the varying rate parameter  $\gamma_i$  under the queue stability condition [1]. For the case of  $d'_{i,1} \geq d_{i,2}$ , there is no queueing delay for packet processing at  $V_2$ . We approximate the packet arrival process of each flow at  $V_2$  as a Poisson process with rate parameter  $\gamma_i$ , and establish an M/D/1 queueing model to determine the average queueing delay before processing at  $V_2$ . Proposition 2 in [1] indicates that the average packet queueing delay, based on the approximated M/D/1 queueing model, provides a more accurate upper bound than that using the G/D/1 queueing model under both lightly- and heavily-loaded input traffic. Therefore, the approximated average packet delay  $D_{i,2}$ , for traffic flow  $i$  traversing  $V_2$  can be determined [1].

In general, the same queueing modeling methodology can be applied independently at each subsequent NFV node (if any) along the embedded network path, upon which an approximated M/D/1 queueing network is established to calculate the E2E packet delay for each embedded VNF chain. With the proposed analytical E2E packet delay modeling, the delay-aware SDT design can be achieved as illustrated in the flowchart in Fig. 5. First, multiple VNF chains for different

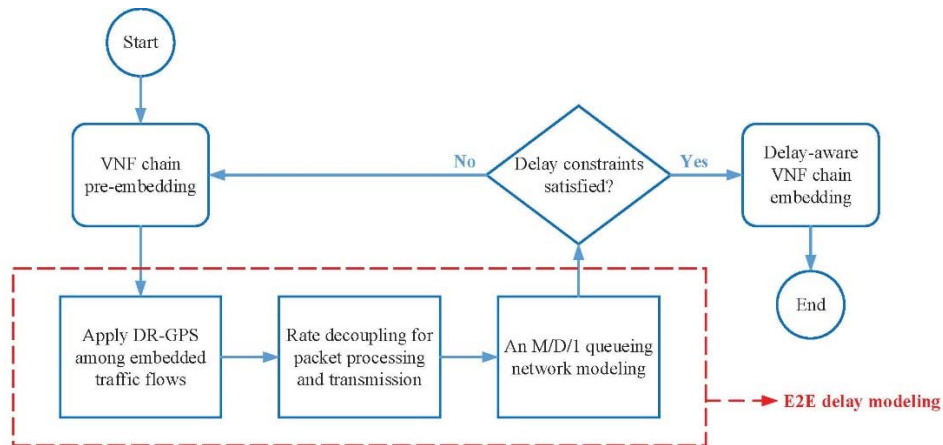


Fig. 5: A diagram illustrating the delay-aware SDT design process.

E2E service requests are pre-embedded on the substrate network. Then, our proposed delay modeling framework is applied to determine the E2E packet delay for traffic flows traversing the embedded VNF chains. If the E2E packet delay constraints for the flows are satisfied, the delay-aware VNF chain embedding process is completed; otherwise, the VNF chain pre-embedding phase is revisited and the whole process is repeated until delay-aware SDT is achieved.

#### 4. Simulation Results

In this section, simulation results are provided to verify the accuracy of the proposed E2E packet delay modeling for embedded VNF chains. All simulations are conducted using OMNeT++ [9]. We consider two VNF chains embedded over a common physical network path, as shown in Fig. 1, where flow  $i$  traverses  $f_1$  and  $f_3$  and flow  $j$  traverses  $f_1$  and  $f_2$ . We test time profiles of the service flows traversing different VNFs over OpenStack [10], a resource virtualization platform for VNF chain orchestration. The testing results and other simulation settings are referred in [1]. We verify the effectiveness of the proposed rate decoupling and delay modeling methods at each NFV node. Packet queueing delay for one of the flows (flow  $j$ ) before processing at  $V_1$  is shown in Fig. 6. It can be seen that the queueing delay derived using the rate decoupling method is close to the simulation results with rate coupling. Packet queueing delay for flow  $j$  at  $V_2$  is evaluated in Fig. 7, where the queueing delay derived based on the approximated M/D/1 queueing model achieves a much tighter upper bound than that using the G/D/1 queueing model.

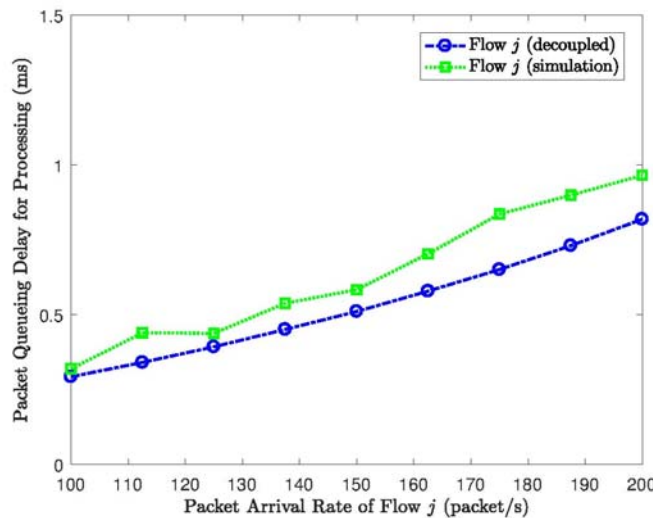


Fig. 6: Average packet queueing delay for processing at  $V_1$ .

#### 5. Conclusion

In this article, an E2E packet delay modeling framework is established for embedded VNF chains over the 5G core network to facilitate delay-aware SDT design. For the VNF chains sharing resources over a common embedded physical network path, the DR-GPS scheme is employed to

allocate the computing resources on network servers and bandwidth resources on outgoing transmission links to achieve dominant resource allocation fairness and high resource utilization. With DR-GPS, an approximated M/D/1 queueing network model is established to analyze the E2E packet delay for traffic flows passing through each embedded VNF chain, which is proved to be more accurate than the G/D/1 queueing model for flows traversing each subsequent NFV node following the first NFV node. Simulation results demonstrate the accuracy and effectiveness of the proposed E2E delay modeling framework, upon which delay-aware SDT can be achieved.

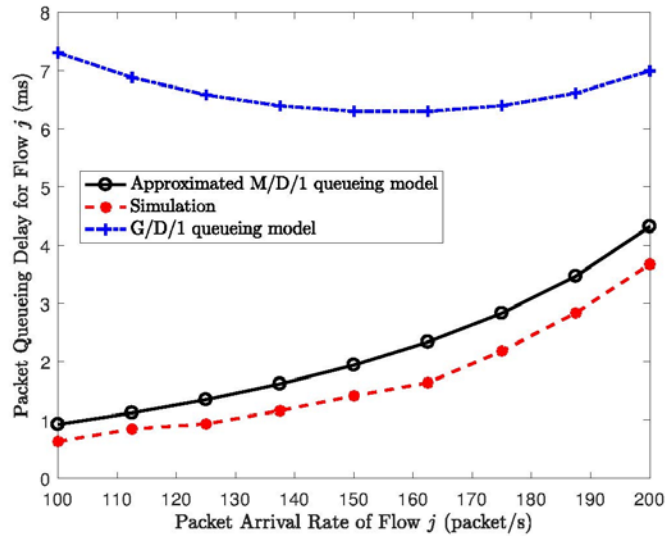


Fig. 7: Average packet queueing delay for processing at  $V_2$ .

## Acknowledgment

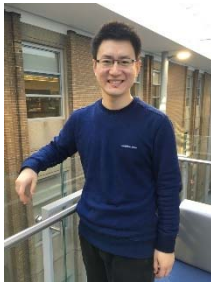
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